

## Class Test

### (STR-Mass Energy Equivalence & Four Vectors)

Q1. According to the special theory of relativity, the speed  $v$  of a free particle of mass  $m$  and total energy  $E = 2mc^2$  is:

- (a)  $\frac{\sqrt{3}}{2}c$                       (b)  $\frac{1}{2}c$                       (c)  $\frac{\sqrt{5}}{4}c$                       (d)  $\frac{1}{4}c$

Q2. The muon has rest mass  $105MeV/c^2$  and mean life time  $2\mu s$  in its rest frame. The mean time traversed by a muon of energy  $210MeV$  before decaying is approximately:

- (a)  $2\mu s$                       (b)  $3\mu s$                       (c)  $4\mu s$                       (d)  $6\mu s$

Q3. A particle of mass  $M$  decays at rest into a massless particle and another particle of mass  $\frac{M}{2}$ . The magnitude of the momentum of each of these relativistic particles is:

- (a)  $\frac{\sqrt{3}}{2}Mc$                       (b)  $\frac{\sqrt{3}}{4}Mc$                       (c)  $\frac{\sqrt{3}}{8}Mc$                       (d)  $\sqrt{3}Mc$

Q4. A particle of rest mass  $m_0$  whose total energy is twice the rest mass energy collide with identical particle at rest. If the stick together and make a composite mass. Find the rest mass of composite mass .

- (a)  $2m_0$                       (b)  $4m_0$                       (c)  $\sqrt{3}m_0$                       (d)  $\sqrt{6}m_0$

Q5. From the S frame total energy and momentum is given by  $E$  and  $\vec{p} = (p_x, p_y, p_z)$  respectively. If another frame  $S'$  is moving with velocity  $v\hat{j}$  then Total energy from  $S'$  frame is

- (a)  $E' = \frac{E - vp_x}{\sqrt{1 - \frac{v^2}{c^2}}}$                       (b)  $E' = \frac{E + vp_x}{\sqrt{1 - \frac{v^2}{c^2}}}$                       (c)  $E' = \frac{E - vp_y}{\sqrt{1 - \frac{v^2}{c^2}}}$                       (d)  $E' = \frac{E + vp_y}{\sqrt{1 - \frac{v^2}{c^2}}}$

Q6. A relativistic particle of mass  $m$  and charge  $e$  is moving in a uniform electric field of strength  $\epsilon$ . Starting from rest at  $t = 0$ , how much time will it take to reach the speed  $\frac{c}{2}$ ?

- (a)  $\frac{1}{\sqrt{3}} \frac{mc}{e\epsilon}$                       (b)  $\frac{mc}{e\epsilon}$                       (c)  $\sqrt{2} \frac{mc}{e\epsilon}$                       (d)  $\sqrt{\frac{3}{2}} \frac{mc}{e\epsilon}$

- Q7. The light source is moving towards observer with velocity  $\frac{\sqrt{3}}{2}c$  at angle  $\theta = 30^\circ$ . If  $\nu_0$  is frequency at rest frame of source. The frequency measured by observer is  
 (a)  $\nu_0$                       (b)  $1.5\nu_0$                       (c)  $2\nu_0$                       (d)  $3\nu_0$
- Q8. If  $x', t'$  is position and time measured from  $S'$  frame and  $x, t$  are measured from  $S$  frame if origin of  $S'$  moving with respect to  $S$  frame. if  $\beta = \frac{v}{c}$  Then  $\frac{\text{one } x' \text{ unit}}{\text{one } x \text{ unit}}$  given by  
 (a) 1                      (b)  $\beta$                       (c)  $\sqrt{\frac{1+\beta^2}{1-\beta^2}}$                       (d)  $\sqrt{\frac{1-\beta^2}{1+\beta^2}}$
- Q9. If  $\vec{A} = (A_0, A_1, A_2, A_3), \vec{B} = (B_0, B_1, B_2, B_3)$  are four vectors the inner product  $\vec{A} \cdot \vec{B}$  is defined as  
 (a)  $\vec{A} \cdot \vec{B} = A_0B_0 + A_1B_1 + A_2B_2 + A_3B_3$                       (b)  $\vec{A} \cdot \vec{B} = A_0B_0 - A_1B_1 - A_2B_2 - A_3B_3$   
 (c)  $\vec{A} \cdot \vec{B} = -A_0B_0 - A_1B_1 - A_2B_2 - A_3B_3$                       (d)  $\vec{A} \cdot \vec{B} = -A_0B_0 + A_1B_1 - A_2B_2 + A_3B_3$
- Q10. An inertial frame  $K'$  moves with a constant speed  $v$  with respect to another inertial frame  $K$  along their common  $x$ -direction. Let  $(x, ct)$  and  $(x', ct')$  denote the space-time coordinates in the frames  $K$  and  $K'$ , respectively. Which of the following space-time diagrams correctly describes the  $t'$ -axis ( $x' = 0$  line) and the  $x'$ -axis ( $t' = 0$  line) in the  $x$ - $ct$  plane? (In the following figures  $\tan \phi = v/c$ )

