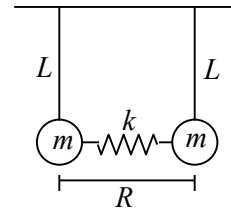


**JNU (M.Sc) Entrance Examination, 2016**

Q1. The maximum radius ( $R_0$ ) that a black hole can have depends on its mass ( $M$ ), the universal constant of gravitation ( $G$ ) and the speed of light ( $c$ ). On dimensional grounds, the expression for  $R_0$  should be proportional to

- (a)  $GM/c^2$                       (b)  $GM^2/c^3$                       (c)  $GM^2/c$                       (d)  $GM/c$   
 (e)  $G^2M/c$

Q2. Two pendulums of identical length  $L$  and mass  $m$  are hanging from a horizontal rod. Their points of suspension are separated by  $R$ . A spring of unstretched length  $R$  and spring constant  $k$ , is now used to connect the masses. For this new system there is a mode of oscillation in which both the masses move sinusoidally with a common circular frequency  $\omega$  and the displacements of the two masses are equal in magnitude but opposite in sign at all times. If  $\omega$  has to be twice the common circular frequency of the two masses before the spring is connected, then the ratio  $\frac{kL}{mg}$ , where  $g$  is the acceleration due to gravity, must be

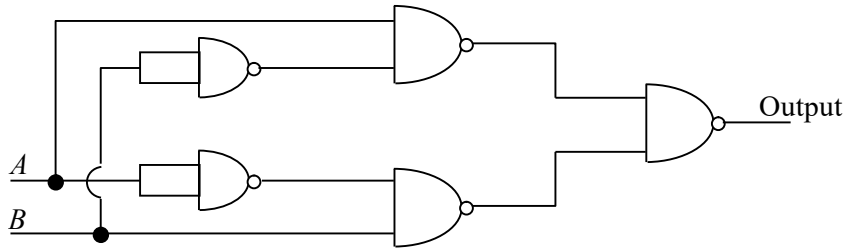


- (a) 1                                      (b)  $\frac{3}{2}$                                       (c) 2                                      (d)  $\frac{2}{3}$   
 (e)  $\sqrt{2}$

Q3. Consider an elastic collision between two objects  $A$  and  $B$  of mass  $m_1$ , and  $m_2$ , respectively. Before and after collision, motion takes place only along the  $x$ -axis. Before collision,  $A$  is moving with speed  $v$  and  $B$  is at rest. If, after collision,  $A$  keeps moving in the same direction, but with its speed reduced to  $\frac{v}{2}$ , the ratio  $\frac{m_2}{m_1}$  must be

- (a) 2                                      (b) 1                                      (c)  $\frac{1}{3}$                                       (d)  $\sqrt{5}-1$   
 (e)  $\sqrt{2}-1$

- Q4. Which of the following represents the output of the circuit implemented using only NAND gates?



- (a)  $A \text{ AND } B$       (b)  $A \text{ OR } B$       (c)  $A \text{ NAND } B$       (d)  $A \text{ NOR } B$   
 (e)  $A \text{ XOR } B$
- Q5. Graphite, an allotrope of carbon, crystallizes in a simple hexagonal crystal structure with primitive translation vectors of the hexagonal space lattice given by

$$a_1 = \frac{\sqrt{3}}{2} a \hat{x} + \frac{a}{2} \hat{y}; a_2 = -\frac{\sqrt{3}}{2} a \hat{x} + \frac{a}{2} \hat{y}; a_3 = c \hat{z}$$

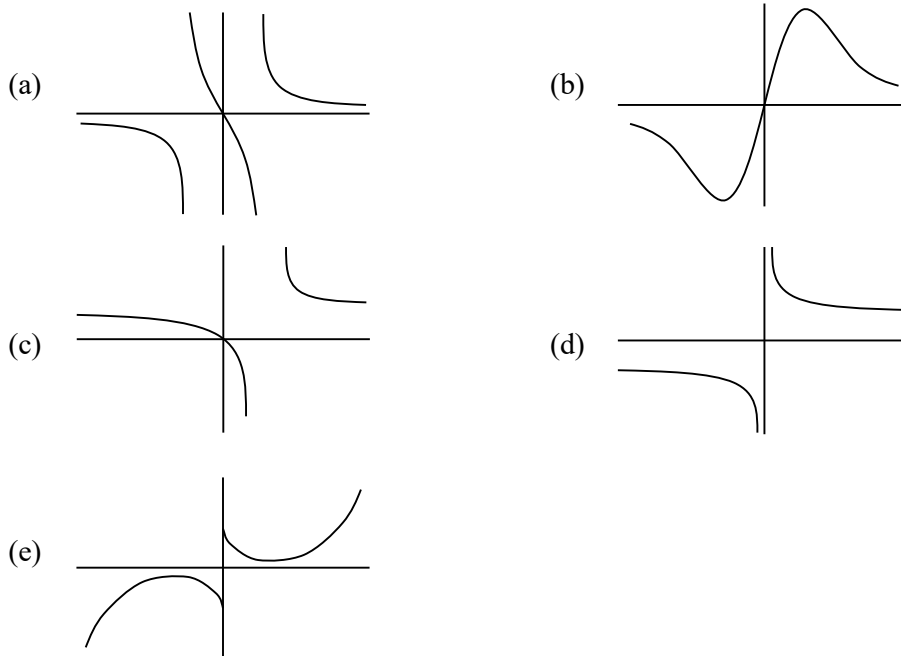
here  $a = 2.46 \text{ \AA}$  and  $c = 6.7 \text{ \AA}$ . Given that there is one atom in the primitive cell, the density of graphite is given by (Take the mass number of carbon to be 12)

- (a)  $0.56 \text{ gm/cm}^3$       (b)  $5.10 \text{ gm/cm}^3$   
 (c)  $2.40 \text{ gm/cm}^3$       (d)  $1.40 \text{ gm/cm}^3$   
 (e)  $4.32 \text{ gm/cm}^3$
- Q6. A solid square slab of dielectric material with dielectric constant 5.0 fills up the space between the two square (5 cm x 5 cm) metallic plates of a capacitor. A potential difference of 10 volts is maintained between the two metal plates which are separated by 1 mm. Suppose the dielectric slab is now pulled out at a speed of 1 mm/s parallel to one of the edges of the plates, with negligible friction. The power required to do this is nearest to
- (a)  $9.00 \times 10^{-11} \text{ W}$       (b)  $1.11 \times 10^{-11} \text{ W}$   
 (c)  $0.22 \times 10^{-11} \text{ W}$       (d)  $4.90 \times 10^{-12} \text{ W}$   
 (e)  $2.16 \times 10^{-12} \text{ W}$
- Q7. Consider a free quantum particle of mass  $m$  in a two-dimensional rectangular box covering the region  $\{0 < x < 2L, 0 < y < L\}$ . In the first excited state, the probability for the particle to be found in  $\{L/2 < x < L, 0 < y < 3L/4\}$  is nearest to

- (a) 0.13      (b) 0.19      (c) 0.16      (d) 0.23  
 (e) 0.27

Q8. Which of the following figures provides the most accurate representation of the function

$$f(x) = \frac{x}{(x^2 - 1)} ?$$



Q9. Cerenkov radiation is observed when the speed of a charged particle in a liquid is greater than the speed of light in that medium. In a liquid of refractive index 1.5, what is the minimum kinetic energy that an electron must have to give out Cerenkov radiation?

- (a) 0.11 MeV      (b) 0.17 MeV      (c) 1.20 MeV      (d) 0.51 MeV  
 (e) 0.61 MeV

Q10. Consider the following differential equation

$$\frac{d^3 y}{dx^3} - 3 \frac{d^2 y}{dx^2} + 2 \frac{dy}{dx} = 0$$

it is given that  $\frac{d^2 y}{dx^2} = 1$ ,  $\frac{dy}{dx} = 0$  and  $y = 1$  at  $x = 0$ . Then the value of  $y$  at  $x = 2$  is nearest to

- (a) 30      (b) 42      (c) 21      (d) 63  
 (e) 12

Q11. Define  $I$  to be the value of the surface integral  $(\int E \cdot dS$ , where  $dS$  points outwards from the domain of integration) of a vector field  $E(E = (x + y^2)i + (z^3 + y^3)j + (x + z^4)k)$  over the entire surface of a cube which bounds the region  $(0 < x < 2, -1 < y < 1, 0 < z < 2)$ . The value of  $I$  is

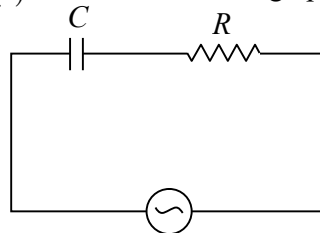
- (a) 0      (b) 16      (c) 72      (d) 80  
 (e) 32





- Q18. A particle of mass  $m$  is moving in a potential field given by  $V(r) = (2x^2 + y^3 + 2z^2)$ . Out of the dynamical variables energy ( $E$ ) and the three components of angular momentum ( $L_x, L_y, L_z$ ), which of the following represents the complete set of conserved quantities?
- (a)  $E$  and  $L_z$                       (b)  $E, L_x$  and  $L_z$                       (c)  $E, L_x, L_y$  and  $L_z$   
 (d)  $E$  and  $L_x$                       (e)  $E$  and  $L_y$

- Q19. In the following a.c. circuit  $R = 10000\Omega, C = 0.32\mu F$ , the frequency of the voltage ( $f$ ) = 50 Hz and the root-mean-square value of  $V(t) = 100 V$ . The average power absorbed by the resistor is nearest to



$$V(t) = V_0 \sin(2\pi ft)$$

- (a) 50 W                      (b) 0.1 W                      (c) 1 W                      (d) 0.5 W  
 (e) 10 W
- Q20. Three moles of an ideal monatomic gas occupy a volume of  $20 m^3$  at  $300 K$ . If the gas expands adiabatically to  $40 m^3$  the final pressure is nearest to
- (a)  $331 N/m^2$                       (b)  $1200 N/m^2$                       (c)  $980 N/m^2$                       (d)  $486 N/m^2$   
 (e)  $118 N/m^2$
- Q21. Ganymede is a moon of the planet Jupiter. It moves in a circular (orbit of radius 1.07 million kilometres with a time period of rotation of 7 days. The mass of Jupiter, deduced from this information, would be nearest to
- (a)  $5.3 \times 10^{29} kg$                       (b)  $1.2 \times 10^{31} kg$   
 (c)  $4.8 \times 10^{28} kg$                       (d)  $1.9 \times 10^{27} kg$   
 (e)  $3.2 \times 10^{30} kg$
- Q22. An ice cube (of mass  $5 gm$ ), at a temperature of  $-23^\circ C$ , is dropped into a lake whose temperature is  $27^\circ C$ . After equilibrium is established, what is the change: in the entropy of the universe nearest to? [Latent heat of fusion for the melting of ice  $80 cal/gm$ , specific heat of water =  $1 cal/gm^\circ C$ , specific heat of ice =  $0.5 cal/gm^\circ C$ ]
- (a)  $1.4 J/K$                       (b)  $9.1 J/K$                       (c)  $0.8 J/K$                       (d)  $8.2 J/K$   
 (e)  $3.6 J/K$

