Pravegae Education

#### **CSIR-NET December 2023**

QID 705015:

A small bar magnet is placed in a magnetic field  $B(\vec{r}) = B(x)\hat{z}$ . The magnet is initially at rest with its magnetic moment along  $\hat{y}$ . At later times, it will undergo

1. angular motion in the yz plane and translational motion along  $\hat{y}$ 

2. angular motion in the yz plane and translational motion along  $\hat{x}$ 

3. angular motion in the zx plane and translational motion along  $\hat{z}$ 

4. angular motion in the xy plane and translational motion along  $\hat{z}$ 

QID 705016:

Each allowed energy level of a system of non-interacting fermions has a degeneracy M. If there are N fermions and R is the remainder upon dividing N by M, then the degeneracy of the ground state is

1.  $R^M$  2. 1 3. M 4.  ${}^M C_R$ 

QID 705011:

The Beta function is defined as  $B(x, y) = \int_0^1 t^{x-1} (1-t)^{y-1} dt$ .

Then B(x, y + 1) + B(x + 1, y) can be expressed as

1. B(x, y - 1) 2. B(x + y, 1) 3. B(x + y, x - y) 4. B(x, y)

QID 705005:

A particle moves in a circular orbit under a force field given by  $\vec{F}(\vec{r}) = -\frac{k}{r^2}\hat{r}$ , where k is a positive constant. If the force changes suddenly to  $\vec{F}(\vec{r}) = -\frac{k}{2r^2}\hat{r}$ , the shape of the new orbit would be

1. parabolic2. Circular3. elliptical4. hyperbolic

#### QID 705002:

The 1-dimensional Hamiltonian of a classical particle of mass m is

$$H = \frac{p^2}{2m}e^{-x/a} + V(x)$$

where a is a constant with appropriate dimensions. The corresponding Lagrangian is,

1. 
$$\frac{m}{2} \left(\frac{dx}{dt}\right)^2 e^{x/a} - V(x)$$
  
3.  $\frac{3m}{2} \left(\frac{dx}{dt}\right)^2 e^{x/a} - V(x)$   
4.  $\frac{3m}{2} \left(\frac{dx}{dt}\right)^2 e^{-x/a} - V(x)$ 

#### QID 705017:

A one-dimensional infinite long wire with uniform linear charge density  $\lambda$ , is placed along the *z*-axis. The potential difference  $\delta V = V(\rho + a) - V(\rho)$ , between two points at radial distances  $\rho + a$  and  $\rho$  from the *z*-axis, where  $a \ll \rho$ , is closest to

$$1. - \frac{\lambda}{2\pi\varepsilon_0} \frac{a^2}{\rho^2} \qquad 2. - \frac{\lambda}{2\pi\varepsilon_0} \frac{a}{\rho} \qquad 3. \frac{\lambda}{2\pi\varepsilon_0} \frac{a}{\rho} \qquad 4. \frac{\lambda}{2\pi\varepsilon_0} \frac{a^2}{\rho^2}$$

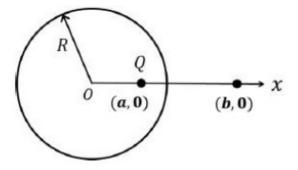
#### QID 705018:

A classical ideal gas is subjected to a reversible process in which its molar specific heat changes with temperature T as  $C(T) = C_V + R \frac{T}{T_0}$ . If the initial temperature and volume are  $T_0$  and  $V_0$ , respectively, and the final volume is  $2V_0$ , then the final temperature is

1.  $T_0/\ln 2$  2.  $2T_0$  3.  $T_0/[1 - \ln 2]$  4.  $T_0[1 + \ln 2]$ 

QID 705016:

A conducting shell of radius R is placed with its centre at the origin as shown below. A point charge Q is placed inside the shell at a distance a along the x-axis from the centre.



The electric field at a distance b > R along the *x*-axis from the centre is

$$1. \frac{Q}{4\pi\varepsilon_0 b^2} \hat{x} \qquad 2. \frac{Q}{4\pi\varepsilon_0} \left[ \frac{1}{(b-a)^2} - \frac{aR}{(ab-R^2)^2} \right] \hat{x} \qquad 3. \frac{Q}{4\pi\varepsilon_0} \left[ \frac{1}{(b-a)^2} + \frac{aR}{(ab-R^2)^2} \right] \hat{x} \qquad 4. \frac{Q}{4\pi\varepsilon_0} \left[ \frac{1}{b^2} - \frac{R^2}{a^2 b^2} \right] \hat{x}$$

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QID 705001:

A particle of mass m is moving in a stable circular orbit of radius  $r_0$  with angular momentum L. For a potential energy  $V(r) = \beta r^k (\beta > 0$  and k > 0), which of the following options is correct?

1. 
$$k = 3, r_0 = \left(\frac{3L^2}{5m\beta}\right)^{1/5}$$
  
2.  $k = 2, r_0 = \left(\frac{L^2}{2m\beta}\right)^{1/4}$   
3.  $k = 2, r_0 = \left(\frac{L^2}{4m\beta}\right)^{1/4}$   
4.  $k = 3, r_0 = \left(\frac{5L^2}{3m\beta}\right)^{1/5}$ 

QID 705025:

The light incident on a solar cell has a uniform photon flux in the energy range of 1eV to 2eV and is zero elsewhere. The active layer of the cell has a bandgap of 1.5eV and absorbs 80% of the photons with energies above the bandgap. Ignoring non-radiative losses, the power conversion efficiency (ratio of the output power to the input power) is closest to

 1. 47%
 2. 70%
 3. 23%
 4. 35%

QID 705006:

The Schrödinger wave function for a stationary state of an atom in spherical polar coordinates  $(r, \theta, \phi)$  is

$$\psi = Af(r)\sin\theta\cos\theta e^{i\phi}$$

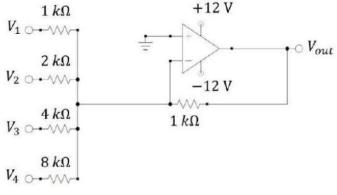
where A is the normalization constant. The eigenvalue of  $\widehat{L_z}$  for this state is

1.  $2\hbar$  2.  $\hbar$  3.  $-2\hbar$  4.  $-\hbar$ 

QID 705006:

In the circuit shown below using an ideal op-amp, inputs  $V_j$  (j = 1,2,3,4) may either be open or

connected to a - 5 V battery.

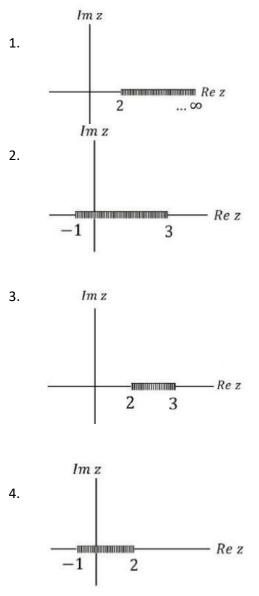


The minimum measurement range of a voltmeter to measure all possible values of  $V_{\rm out}$  is

1. 10V 2. 30V 3. 3V 4. 1V

## QID 705010:

The branch line for the function 
$$f(z) = \sqrt{((z^2 - 5z + 6)/(z^2 + 2z + 1))}$$
 is



QID 705004:

The coordinates of the following events in an observer's inertial frame of reference are as follows: Event 1:  $t_1 = 0$ ,  $x_1 = 0$ : A rocket with uniform velocity 0.5c crosses the observer at origin along x axis

Event 2:  $t_2 = T$ ,  $x_2 = 0$ : The observer sends a light pulse towards the rocket

Event 3:  $t_3$ ,  $x_3$ : The rocket receives the light pulse

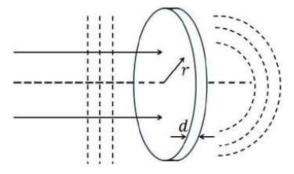
The values of  $t_3$ ,  $x_3$  respectively are



1. 2*T*, *cT* 2. 2*T*, 
$$\frac{c}{2}T$$
 3.  $\frac{\sqrt{3}}{2}T$ ,  $\frac{2}{\sqrt{3}}cT$  4.  $\frac{2}{\sqrt{3}}T$ ,  $\frac{\sqrt{3}}{2}cT$ 

QID 705014:

For a flat circular glass plate of thickness d, the refractive index n(r) varies radially, where r is the radial distance from the centre of the plate. A coherent plane wavefront is normally incident on this plate as shown in the figure below.



If the emergent wavefront is spherical and centered on the axis of the plate, then n(r) - n(0)should be proportional to

1.  $r^{1/2}$  2. r 2.  $r^2$  4.  $r^{3/2}$ 

QID 705007:

The Hamiltonian for two particles with angular momentum quantum numbers  $l_1 = l_2 = 1$ , is

$$\widehat{H} = \frac{\epsilon}{h^2} \Big[ \left( \widehat{L}_1 + \widehat{L}_2 \right) \cdot \widehat{L}_2 - \left( \widehat{L}_{1z} + \widehat{L}_{2z} \right)^2 \Big].$$

If the operator for the total angular momentum is given by  $\hat{L} = \hat{L}_1 + \hat{L}_2$ , then the possible energy eigenvalues for states with l = 2, (where the eigenvalues of  $\hat{L}^2$  are  $l(l+1)\hbar^2$ ) are

1.  $3\epsilon, 2\epsilon, -\epsilon$  2.  $6\epsilon, 5\epsilon, 2\epsilon$  3.  $3\epsilon, 2\epsilon, \epsilon$  4.  $-3\epsilon, -2\epsilon, \epsilon$ 

QID 705021:

A system of N non-interacting classical spins, where each spin can take values  $\sigma = -1,0,1$ , is placed in a magnetic field h. The single spin Hamiltonian is given by

$$H = -\mu_B h \sigma + \Delta (1 - \sigma^2),$$

where  $\mu_B, \Delta$  are positive constants with appropriate dimensions. If M is the magnetization, the zero-field magnetic susceptibility per spin  $\frac{1}{N} \frac{\partial M}{\partial h}\Big|_{h\to 0}$ , at a temperature  $T = 1/\beta k_B$  is given by

1.  $\beta \mu_B^2$  2.  $\frac{2\beta \mu_B^2}{2+e^{-\beta \Delta}}$  3.  $\beta \mu_B^2 e^{-\beta \Delta}$  4.  $\frac{\beta \mu_B^2}{1+e^{-\beta \Delta}}$ 

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QID 705008:

The normalized wave function of an electron is

$$\psi(\vec{r}) = R(r) \left[ \sqrt{\frac{3}{8}} Y_1^0(\theta, \varphi) \chi_- + \sqrt{\frac{5}{8}} Y_1^1(\theta, \varphi) \chi_+ \right],$$

where  $Y_l^m$  are the normalized spherical harmonics and  $\chi_{\pm}$  denote the wavefunction for the two spin states with eigenvalues  $\pm \frac{1}{2}\hbar$ . The expectation value of the *z* component of the total angular momentum in the above state is

1. 
$$-\frac{3}{4}\hbar$$
 2.  $\frac{3}{4}\hbar$  3.  $-\frac{9}{8}\hbar$  4.  $\frac{9}{8}\hbar$ 

QID 705020:

Four distinguishable particles fill up energy levels  $0, \epsilon, 2\epsilon$ . The number of available microstates for the total energy  $4\epsilon$  is

1. 20 2. 24 3. 11 4. 19

QID 705012:

If z is a complex number, which among the following sets is neither open nor closed?

1.  $\{z \mid 0 \le |z - 1| \le 2\}$ 2.  $\{z \mid z \mid \le 1\}$ 3.  $\{z \mid z \in (\mathbb{C} - \{3\}) \text{ and } |z| \le 100\}$ 4.  $\{z \mid z = re^{i\theta}, 0 \le \theta \le \frac{\pi}{4}\}$ 

QID 705003:

A particle of unit mass subjected to the 1-dimensional potential

$$V(x) = \frac{2\alpha}{x^3} - \frac{3\beta}{x^2}$$

executes small oscillations about its equilibrium position, where  $\alpha$  and  $\beta$  are positive constants with appropriate dimensions. The time period of small oscillations is

1. 
$$\frac{\pi\alpha^2}{\sqrt{6\beta^5}}$$
 2.  $\frac{\pi\alpha^2}{\sqrt{3\beta^5}}$  3.  $\frac{2\pi\alpha^2}{\sqrt{3\beta^5}}$  4.  $\frac{2\pi\alpha^2}{\sqrt{6\beta^5}}$ 

QID 705023:

For three inputs *A*, *B* and *C*, the minimum number of 2-input NAND gates required to generate the output  $Y = \overline{A + B} + \overline{C}$  is

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#### QID 705009:

A quantum system is described by the Hamiltonian

$$H = JS_z + \lambda S_x$$

where  $S_i = \frac{\hbar}{2}\sigma_i$  and  $\sigma_i(i = x, y, z)$  are the Pauli matrices. If  $0 < \lambda \ll J$ , then the leading correction in  $\lambda$  to the partition function of the system at temperature T is

1.  $\frac{\hbar\lambda^2}{2Jk_BT} \operatorname{coth}\left(\frac{J\hbar}{2k_BT}\right)$ 2.  $\frac{\hbar\lambda^2}{2Jk_BT} \tanh\left(\frac{J\hbar}{2k_BT}\right)$ 3.  $\frac{\hbar\lambda^2}{2Jk_BT} \cosh\left(\frac{J\hbar}{2k_BT}\right)$ 4.  $\frac{\hbar\lambda^2}{2Jk_BT} \sinh\left(\frac{J\hbar}{2k_BT}\right)$ 

QID 705009:

Let *M* be a  $3 \times 3$  real matrix such that

$$e^{M\theta} = \begin{bmatrix} \cos\theta & \sin\theta & 0\\ -\sin\theta & \cos\theta & 0\\ 0 & 0 & 1 \end{bmatrix},$$

where  $\theta$  is a real parameter. Then *M* is given by

[-1	0	0]	ΓO	1	[0		0		[1	0	[0
$1.\begin{bmatrix} -1\\0\\0\end{bmatrix}$	1	0	$2 \begin{bmatrix} 0 \\ -1 \end{bmatrix}$	0	0	3. 0	-1	0	4. 0	$\begin{array}{c} 0 \\ -1 \\ 0 \end{array}$	0
Lo	0	0]	Lo	0	0]	Lo	0	0]	Lo	0	1

QID 705022:

In the measurement of a radioactive sample, the measured counts with and without the sample for equal time intervals are C = 500 and B = 100, respectively. The errors in the measurements of C and B are  $|\Delta C| = 20$  and  $|\Delta B| = 10$ , respectively. The net error  $|\Delta Y|$  in the measured counts from the sample Y = C - B, is closest to

1. 22 2. 10 3. 30 4. 43

QID 705027:

A canonical transformation from the phase space coordinates (q, p) to (Q, P) is generated by the function

$$\psi(p,Q) = \frac{p^2}{2\omega} \tan 2\pi Q,$$

where  $\omega$  is a positive constant. The function  $\psi(p,Q)$  is related to F(q,Q) by the Legendre transform  $\psi = pq - F$ , where F is defined by dF = pdq - PdQ. If the solution for (P,Q) is

$$P(t) = \frac{\omega}{4\pi}t^2, Q(t) = Q_0 = \text{ constant},$$

where t is time, then the solution for (p, q) variables can be written as

1. 
$$p = \frac{\omega t}{2\pi} \cos 2\pi Q_0, q = \frac{t}{2\pi} \sin 2\pi Q_0$$
 2.  $p = -\frac{\omega t}{2\pi} \cos 2\pi Q_0, q = \frac{t}{2\pi} \sin 2\pi Q_0$ 

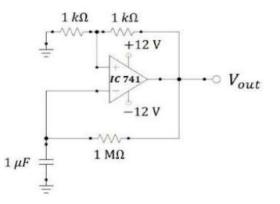
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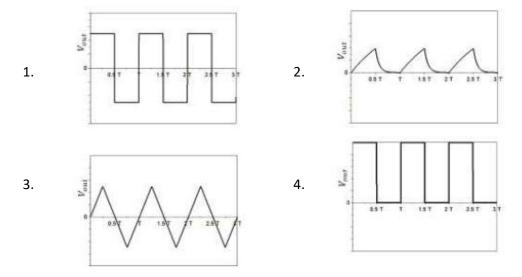
3. 
$$p = \frac{\omega t}{2\pi} \sin 2\pi Q_0, q = \frac{t}{2\pi} \cos 2\pi Q_0$$
 4.  $p = -\frac{\omega t}{2\pi} \sin 2\pi Q_0, q = \frac{t}{2\pi} \cos 2\pi Q_0$ 

QID 705045:

A circuit with operational amplifier is shown in the figure below.



The output voltage waveform  $V_{out}$  will be closest to



QID 705052:

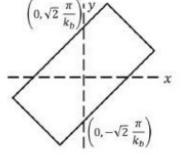
In the rotational-vibrational spectrum of an idealized carbon monoxide (CO) molecule, ignoring rotational-vibrational coupling, two transitions between adjacent vibrational levels with wavelength  $\lambda_1$  and  $\lambda_2$ , correspond to the rotational transition from J' = 0 to J'' = 1, and J' = 1 to J'' = 0, respectively. Given that the reduced mass of *CO* is  $1.2x^{-26}$  kg, equilibrium bond length of *CO* is 0.12 nm and vibrational frequency is  $5 \times 10^{13}$  Hz, the ratio of  $\frac{\lambda_1}{\lambda_2}$  is closest to 1.0.9963 2.0.0963 3.1.002 4.1.203

# QID 705040:

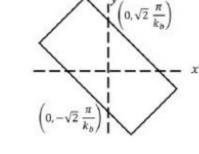
A 2-dimensional resonant cavity supports a TM mode built from a function

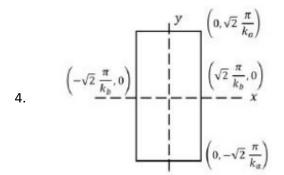
 $\psi(x, y, t) = \sin(\vec{k}_a \cdot \vec{r} - \omega t) + \sin(\vec{k}_b \cdot \vec{r} - \omega t) + \sin(\vec{k}_a \cdot \vec{r} + \omega t) + \sin(\vec{k}_b \cdot \vec{r} + \omega t)$ where  $\vec{k}_a$  and  $\vec{k}_b$  lie in the *xy*-plane and make angles  $\frac{\pi}{4}$  and  $\frac{3\pi}{4}$  with the *x*-axis, respectively. If  $0 < |\vec{k}_a| < |\vec{k}_b|$ , then which of the following closely describes the outline of the cavity?

2.









#### QID 705031:

A quantum particle of mass m is moving in a one dimensional potential

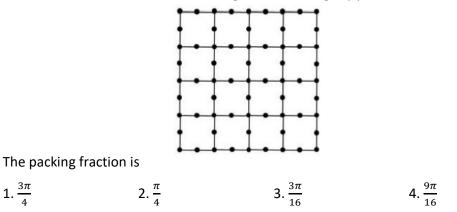
$$V(x) = V_0 \theta(x) - \lambda \delta(x),$$

where  $V_0$  and  $\lambda$  are positive constants,  $\theta(x)$  is the Heaviside step function and  $\delta(x)$  is the Dirac delta function. The leading contribution to the reflection coefficient for the particle incident from the left with energy  $E \gg V_0$  and  $\sqrt{2mE} \gg V_0 h$  is

the left with energy 
$$E \gg V_0 > \lambda$$
 and  $\sqrt{2mE} \gg \frac{V_0 h}{\lambda}$  is  
1.  $\frac{V_0^2}{4E^2}$  2.  $\frac{V_0^2}{8E^2}$  3.  $\frac{m\lambda^2}{2Eh^2}$  4.  $\frac{m\lambda^2}{4Eh^2}$ 

### QID 705049:

In the section of an infinite lattice shown in the figure below, all sites are occupied by identical hard circular discs so that the resulting structure is tightly packed.



QID 705044

Gauge factor of a strain gauge is defined as the ratio of the fractional change in resistance  $\left(\frac{\Delta R}{R}\right)$  to the fractional change in length  $\left(\frac{\Delta L}{L}\right)$ . A metallic strain gauge with a gauge factor 2 has a resistance of 100 $\Omega$  under unstrained condition. An aluminum foil with Young's modulus Y = 70GN/m<sup>2</sup> is installed on the metallic gauge. Keeping the foil within its elastic limit, a stress of 0.2GN/m<sup>2</sup> is applied on the foil. The change in the resistance of the gauge will be closest to

1. 
$$0.14\Omega$$
2.  $1.23\Omega$ 3.  $0.28\Omega$ 4.  $0.56\Omega$ 

In a quantum harmonic oscillator problem,  $\hat{a}$  and  $\hat{N}$  are the annihilation operator and the number operator, respectively. The operator  $e^{\hat{N}}\hat{a}e^{-\hat{N}}$  is

1.  $\hat{a}$  2.  $e^{-1}\hat{a}$  3.  $e^{-(\hat{l}+\hat{a})}$  4.  $e^{\hat{a}}$ 

(where  $\hat{I}$  is the identity operator)

#### QID 705053

Atmospheric neutrinos are produced from the cascading decays of cosmic pions  $(\pi^{\pm})$  to stable particles. Ignoring all other neutrino sources, the ratio of muon neutrino  $(v_{\mu} + \bar{v}_{\mu})$  flux to electron neutrino  $(v_e + \bar{v}_e)$  flux in atmosphere is expected to be closest to

QID 705041

A system of non-relativistic and non-interacting bosons of mass m in two dimensions has a density n. The Bose-Einstein condensation temperature  $T_c$  is

1. 
$$\frac{12n\hbar^2}{\pi m_B}$$
 2. 
$$\frac{3n\hbar^2}{\pi m k_B}$$
 3. 
$$\frac{6n\hbar^2}{\pi m k_B}$$
 4. 0

QID 705047

The lattice constant of the bcc structure of sodium metal is 4.22Å. Assuming the mass of the electron inside the metal to be the same as free electron mass, the free electron Fermi energy is closest to

1. 3.2eV 2. 2.9eV 3. 3.5eV 4. 2.5eV

QID 705033

The regular representation of two nonidentity elements of the group of order 3 are given by

$1.\begin{pmatrix}0\\1\\0\end{pmatrix}$	1 0 0	$\begin{pmatrix} 0\\0\\1 \end{pmatrix}$ , $\begin{pmatrix} 0\\0\\1 \end{pmatrix}$	0 1 0	$\begin{pmatrix} 1\\0\\0 \end{pmatrix}$	2.	$\begin{pmatrix} 1\\0\\0 \end{pmatrix}$	0 0 1	$\begin{pmatrix} 0\\1\\0 \end{pmatrix}, \begin{pmatrix} 0\\1\\0 \end{pmatrix}$	1 0 0	$\begin{pmatrix} 0\\0\\1 \end{pmatrix}$
$3.\begin{pmatrix}0\\1\\0\end{pmatrix}$	0 0 1	$\begin{pmatrix} 1\\0\\0 \end{pmatrix}, \begin{pmatrix} 0\\0\\1 \end{pmatrix}$	1 0 0	$\begin{pmatrix} 0\\1\\0 \end{pmatrix}$	4.	$\begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$	0 1 0	$\begin{pmatrix} 1\\0\\0 \end{pmatrix}, \begin{pmatrix} 0\\1\\0 \end{pmatrix}$	0 0 1	$\begin{pmatrix} 1\\0\\0 \end{pmatrix}$

QID 705032

A quantum system is described by the Hamiltonian

$$H = -J\sigma_z + \lambda(t)\sigma_x,$$

where  $\sigma_i (i = x, y, z)$  are Pauli matrices, J and  $\lambda$  are positive constants  $(J \gg \lambda)$  and

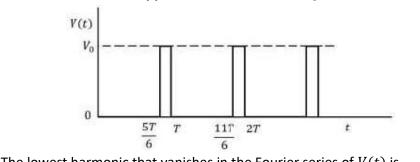
$$\lambda(t) = \begin{cases} 0 & \text{for} \quad t < 0\\ \lambda & \text{for} \quad 0 < t < T\\ 0 & \text{for} \quad t > T \end{cases}$$

At t < 0, the system is in the ground state. The probability of finding the system in the excited state at  $t \gg T$ , in the leading order in  $\lambda$  is

$$1. \frac{\lambda^2}{8J^2} \sin^2 \frac{JT}{\hbar} \qquad 2. \frac{\lambda^2}{J^2} \sin^2 \frac{JT}{\hbar} \qquad 3. \frac{\lambda^2}{4J^2} \sin^2 \frac{JT}{\hbar} \qquad 4. \frac{\lambda^2}{16J^2} \sin^2 \frac{JT}{\hbar}$$

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#### QID 705046



An infinite waveform V(t) varies as shown in the figure below

The lowest harmonic that vanishes in the Fourier series of V(t) is

#### QID 705037

A transmission line has the characteristic impedance of  $(50 + 1j)\Omega$  and is terminated in a load resistance of  $(70 - 7j)\Omega$  (where  $j^2 = -1$ ). The magnitude of the reflection coefficient will be closest to

1. 
$$\frac{5}{7}$$
 2.  $\frac{1}{2}$  3.  $\frac{1}{6}$  4.  $\frac{1}{7}$ 

QID 705035

The function  $f(z) = \frac{1}{(z+1)(z+3)}$  is defined on the complex plane. The coefficient of the  $(z-z_0)^2$ term of the Laurent series of f(z) about  $z_0 = 1$  is

 $1.\frac{7}{64}$ 2.  $\frac{7}{128}$  3.  $\frac{9}{64}$  $4.\frac{9}{128}$ 

### QID 705039

The radius of a sphere oscillates as a function of time as  $R + a\cos \omega t$ , with a < R. It carries a charge Q uniformly distributed on its surface at all times. If P is the time averaged radiated power through a sphere of radius r, such that  $r \gg R + a$  and  $r \gg \frac{c}{\omega}$ , then

1. 
$$P \propto \frac{Q^2 \omega^4 a^2}{c^3}$$
 2.  $P \propto \frac{Q^2 \omega^2}{c}$  3.  $P = 0$  4.  $P \propto \frac{Q^2 \omega^6 a^4}{c^5}$ 

QID 705028

A Lagrangian is given by

$$L = \frac{1}{2}m(\dot{x}^2 + \dot{y}\dot{z} + \dot{z}^2) - \alpha(2x + 3y + z).$$

The conserved momentum is

1. 
$$m[2\dot{x} + \dot{z}]$$
 2.  $m[2\dot{x} + \dot{y} + \dot{z}]$  3.  $m\left[\dot{x} + \frac{3}{2}\dot{y} + \frac{1}{2}\dot{z}\right]$  4.  $m[2\dot{x} + 3\dot{z}]$ 

#### QID 705036

The solution y(x) of the differential equation  $y'' + \frac{y}{4} = \frac{x}{2}$ , where  $0 \le x \le \pi$ , together with the boundary conditions  $y(0) = y(\pi) = 0$  is

$$1. \frac{2}{\pi} \sum_{n=1}^{\infty} (-1)^n \frac{\pi}{n} \frac{\sin nx}{\frac{1}{4} - n^2} \qquad 2. \frac{2}{\pi} \sum_{n=1}^{\infty} (-1)^n \frac{\pi}{2n} \frac{\sin nx}{\frac{1}{4} - n^2} \\ 3. \frac{2}{\pi} \sum_{n=1}^{\infty} (-1)^{n+1} \frac{\pi}{n} \frac{\sin nx}{\frac{1}{4} - n^2} \qquad 4. \frac{2}{\pi} \sum_{n=1}^{\infty} (-1)^{n+1} \frac{\pi}{2n} \frac{\sin nx}{\frac{1}{4} - n^2}$$

#### QID 705029

An incident plane wave with wavenumber k is scattered by a spherically symmetric soft potential. The scattering occurs only in S - and P-waves. The approximate scattering amplitude at angles  $\theta = \frac{\pi}{3}$  and  $\theta = \frac{\pi}{2}$  are

$$f\left(\theta = \frac{\pi}{3}\right) \simeq \frac{1}{2k} \left(\frac{5}{2} + 3i\right)$$
 and  $f\left(\theta = \frac{\pi}{2}\right) \simeq \frac{1}{2k} \left(1 + \frac{3i}{2}\right)$ .

Then the total scattering cross-section is closest to

1. 
$$\frac{37\pi}{4k^2}$$
 2.  $\frac{10\pi}{k^2}$  3.  $\frac{35}{4k^2}$  4.  $\frac{9\pi}{k^2}$ 

QID 705051

A solar probe mission detects a fractional wavelength shift  $(\Delta \lambda / \lambda)$  of the spectral line  $\lambda = 630$  nm within a sunspot to be of the order of  $10^{-5}$ . Assuming this shift is caused by the normal Zeeman effect (i.e., neglecting other physical effects), the estimated magnetic field (in tesla) within the observed sunspot is closest to

1.  $3 \times 10^{-5}$  2. 300 3. 0.3 4.  $3 \times 10^{5}$ 

QID 705043

A photon inside the sun executes a random walk process. Given the radius of the sun  $\approx$  7 × 10<sup>8</sup> km and mean free path of a photon  $\approx$  10<sup>-3</sup> m, the time taken by the photon to travel from the centre to the surface of the sun is closest to

1.  $10^6 \sec$ 2.  $10^{24} \sec$ 3.  $10^{12} \sec$ 4.  $10^{18} \sec$ 

QID 705050

The ionization potential of hydrogen atom is 13.6eV, and  $\lambda_H$  and  $\lambda_D$  denote longest wavelengths in Balmer spectrum of hydrogen and deuterium atoms, respectively. Ignoring the fine and hyperfine structures, the percentage difference  $y = \frac{\lambda_H - \lambda_D}{\lambda_H} \times 100$ , is closest to 1. 1.0003% 2. -0.03% 3. 0.03% 4. -1.0003%

### QID 705048

The collision time of the electrons in a metal in the Drude model is  $\tau$  and their plasma frequency is  $\omega_p$ . If this metal is placed between the plates of a capacitor, the time constant associated with the decay of the electric field inside the metal is

1. 
$$\tau + \frac{1}{\omega_p}$$
 2.  $\omega_p \tau^2$  3.  $\frac{1}{\omega_p^2 \tau}$  4.  $\frac{\tau}{1 + \omega_p \tau}$ 

QID 705034

Given the data points

x	1	3	5		
у	4	28	92		

using Lagrange's method of interpolation, the value of y at x = 4 is closest to

1.54 2.55 3.53 4.56

QID 705026

A particle of mass m is moving in a 3-dimensional potential

$$\phi(r) = -\frac{k}{r} - \frac{k'}{3r^3} \, k, k' > 0.$$

For the particle with angular momentum l, the necessary condition to have a stable circular orbit is

1. 
$$kk' < \frac{l^4}{4m^2}$$
 2.  $kk' > \frac{l^4}{4m^2}$  3.  $kk' < \frac{l^4}{m^2}$  4.  $kk' > \frac{l^4}{m^2}$ 

### QID 705042

The work done on a material to change its magnetization M in an external field H is dW = HdM. Its Gibbs free energy is

$$G(T,H) = -\left(\gamma T + \frac{aH^2}{2T}\right),$$

where  $\gamma, a > 0$  are constants. The material is in equilibrium at a temperature  $T = T_0$  and in an external field  $H = H_0$ . If the field is decreased to  $\frac{H_0}{2}$  adiabatically and reversibly, the temperature changes to

1. 
$$2T_0$$
 2.  $\frac{T_0}{2}$  3.  $\left(\frac{a}{2\gamma}\right)^{\frac{1}{4}}\sqrt{H_0T_0}$  4.  $\left(\frac{a}{\gamma}\right)^{\frac{1}{4}}\sqrt{H_0T_0}$ 

# QID 705054

The ground state of  ${}^{207}_{82}$  Pb nucleus has spin-parity  $J^{\pi} = \left(\frac{1}{2}\right)^{-}$ , while the first excited state has  $J^{\pi} = \left(\frac{5}{2}\right)^{-}$ . For the transition from the first excited state to the ground state, possible multipolarities of emitted electromagnetic radiation are

1. E2, E3 2. M2, M3 3. M2, E3 4. E2, M3

# QID 705055

In a shell model description, neglecting Coulomb effects, which of the following statements for the energy and spin-parity is correct for the first excited state of A = 12 isobars  $\frac{12}{5}$  B,  $\frac{12}{6}$ C,  $\frac{12}{7}$  N?

- 1. same for  ${}^{12}_{5}$  B,  ${}^{12}_{6}$ C and  ${}^{12}_{7}$  N
- 2. different for each  ${}^{12}_5$  B,  ${}^{12}_6$ C and  ${}^{12}_7$  N
- 3. same for  ${}^{12}_6$ C and  ${}^{12}_7$ N, but different for  ${}^{12}_5$ B
- 4. same for  ${}^{12}_5$  B and  ${}^{12}_7$  N, but different for  ${}^{12}_6$ C
- QID 705038

The permittivity of a medium  $\varepsilon(\vec{k},\omega)$ , where  $\omega$  and  $\vec{k}$  are the frequency and wavevector, respectively, has no imaginary part. For a longitudinal wave,  $\vec{k}$  is parallel to the electric field such that  $\vec{k} \times \vec{E} = 0$ , while for a transverse wave  $\vec{k} \cdot \vec{E} = 0$ . In the absence of free charges and free currents, the medium can sustain

- 1. longitudinal waves with  $\vec{k}$  and  $\omega$  when  $\varepsilon(\vec{k},\omega) > 0$
- 2. transverse waves with  $\vec{k}$  and  $\omega$  when  $\varepsilon(\vec{k},\omega) < 0$
- 3. longitudinal waves with  $\vec{k}$  and  $\omega$  when  $\varepsilon(\vec{k},\omega)=0$
- 4. both longitudinal and transverse waves with  $\vec{k}$  and  $\omega$  when  $\varepsilon(\vec{k}, \omega) > 0$