CSIR NET-JRF, GATE, IIT-JAM, JEST, TIFR and GRE for Physics

## TIFR 2024

Q1. Which of the following sheets of paper can be turned into a regular octahedron (a threedimensional regular polyhedron with eight triangular faces, as shown on the right) by folding along the marked lines?

(a)

(c)

(d)


Q2. A surface is given by $2 x^{3} z+4 y^{2} z+3 z^{2}=81$
Which of the following is a vector tangential to it at the point on the surface with coordinates $(x, y, z)=(1,2,3) ?$
(a) $2 \hat{i}-3 \hat{j}+3 \hat{k}$
(b) $18 \hat{i}+48 \hat{j}+36 \hat{k}$
(c) $-3 \hat{i}+2 \hat{j}+6 \hat{k}$
(d) $-3 \hat{i}-2 \hat{j}+6 \hat{k}$

Q3. Consider the following differential equations:

$$
\frac{d x}{d t}=a y(t), \frac{d y}{d t}=a
$$

where $a$ is a positive constant. The solutions to these equations define a family of curves in the $x, y$ plane. What are these curves?
(a) Parabolas
(b) Circles
(c) Hyperbolas
(d) Ellipses

CSIR NET-JRF, GATE, IIT-JAM, JEST, TIFR and GRE for Physics
Q4. Consider a mass $m$ connected to a network of massless springs shown in the figure below.


The spring constant of spring $A$ is $k_{A}$, and that of spring $B$ is $k_{B}$. The springs are shown in a relaxed position, and the angle $\theta$ in this position is $\pi / 3$. The mass is displaced horizontally by a small distance. What is the angular frequency of small oscillations of $m$ (Ignore gravity and friction)
(a) $\sqrt{\left(3 k_{A} k_{B}\right) /\left[m\left(2 k_{B}+3 k_{A}\right)\right]}$
(b) $\sqrt{\left(k_{A} k_{B}\right) /\left[m\left(k_{B}+k_{A}\right)\right]}$
(c) $\sqrt{\left(2 k_{A} k_{B}\right) /\left[m\left(k_{B}+2 k_{A}\right)\right]}$
(d) $\sqrt{\left(\sqrt{3} k_{A} k_{B}\right) /\left[m\left(k_{B}+\sqrt{3} k_{A}\right)\right]}$

Q5. Consider an object falling in air. In addition to gravity, it experiences an air resistance force, $R$, given by $R=b v$, where $v$ is the speed and $b$ is a constant. If the object is dropped from rest ( $v=0$ at $t=0)$, the distance traversed by the object at $t=m / b$ is:
(a) $\left(\frac{m^{2} g}{b^{2}}\right)\left(\frac{1}{e}\right)$
(b) $\left(\frac{m^{2} g}{b^{2}}\right)\left(1-\frac{1}{e}\right)$
(c) $\left(\frac{m^{2} g}{b^{2}}\right)(e-1)$
(d) $\left(\frac{m^{2} g}{b^{2}}\right)\left(2-\frac{1}{e}\right)$

Q6. A frictionless disk of mass $m$ is balanced at rest on the edges of two platforms at points $A$ and $B$ that are at equal height as shown below. The angle made by the line joining the centre to point $A$ (line CA) with the vertical is $\pi / 3$.


What is the magnitude of the force exerted by point A on the disk?
(a) $m g$
(b) $\frac{m g}{2}$
(c) $\frac{m g}{\sqrt{3}}$
(d) $\frac{m g \sqrt{3}}{2}$

CSIR NET-JRF, GATE, IIT-JAM, JEST, TIFR and GRE for Physics
Q7. Consider a particle of mass $m$ moving in a one-dimensional potential of the form

$$
V(x)= \begin{cases}\frac{1}{2} k x^{2} & \text { for } x>0 \\ \infty & \text { for } x \leq 0\end{cases}
$$

In a quantum mechanical treatment, what is the ground state energy of the particle?
(a) $\frac{3}{2} \hbar \sqrt{\frac{k}{m}}$
(b) $\frac{1}{2} \hbar \sqrt{\frac{k}{m}}$
(c) $\hbar \sqrt{\frac{k}{m}}$
(d) $\frac{5}{2} \hbar \sqrt{\frac{k}{m}}$

Q8. The un-normalized energy eigenfunction of a one-dimensional simple quantum harmonic oscillator in dimensionless units ( $m=\hbar=\omega=1$ ) is

$$
\psi_{a}(x)=\left(2 x^{3}-3 x\right) e^{-x^{2} / 2}
$$

Which of the following are two other (un-normalized) eigenfunctions which are closest in energy to $\psi_{a}$ ?
(a) $\left(2 x^{2}-1\right) e^{-x^{2} / 2} ;\left(4 x^{4}-12 x^{2}+3\right) e^{-x^{2} / 2}$
(b) $e^{-x^{2} / 2} ;\left(2 x^{2}-1\right) e^{-x^{2} / 2}$
(c) $x e^{-x^{2} / 2} ;\left(4 x^{5}-20 x^{3}+15 x\right) e^{-x^{2} / 2}$
(d) $\left(2 x^{2}-1\right) e^{-x^{2} / 2} ;\left(4 x^{5}+20 x^{3}+15 x\right) e^{-x^{2} / 2}$

Q9. A quantum-mechanical state of a particle, with Cartesian coordinates $x, y$ and $z$, is described by the normalized wave function $\psi(x, y, z)=\frac{a^{5 / 2}}{\sqrt{\pi}} z e^{-a \sqrt{x^{2}+y^{2}+z^{2}}}$ For this state what are the angular quantum number $\ell, L^{2}$ and $L_{z}$ respectively?
(a) $1 ; 2 \hbar^{2} ; 0$
(b) $0 ; 0 ; 0$
(c) $1 ; 2 \hbar^{2} ; \hbar$
(d) $2 ; 6 \hbar^{2} ; 0$

Q10. A thin spherical shell of radius $R$ has a constant surface charge density $\sigma$. This shell is cut symmetrically into two pieces. What is the electrostatic force between the two halves?
(a) $\frac{\pi}{2} \frac{\sigma^{2} R^{2}}{\varepsilon_{0}}$
(b) $\frac{\pi}{4} \frac{\sigma^{2} R^{2}}{\varepsilon_{0}}$
(c) $\pi \frac{\sigma^{2} R^{2}}{\varepsilon_{0}}$
(d) $2 \pi \frac{\sigma^{2} R^{2}}{\varepsilon_{0}}$

CSIR NET-JRF, GATE, IIT-JAM, JEST, TIFR and GRE for Physics
Q11. Consider a system of three electric charges: (i) a charge $--q$ placed at the point $(x, y, z)=(0,0, d)$ (ii) a charge $+\alpha q$ placed at the origin and (iii) a charge $-\beta q$ placed at the point $(x, y, z)=(0,0,-d)$.


The values of $\alpha$ and $\beta$ are such that the monopole and dipole terms vanish in the multipole expansion of the electrostatic potential.

What is the quadrupole term of the potential at a point $(x, y, 0)$ ?
(a) $\frac{q}{4 \pi \varepsilon_{0}} \frac{d^{2}}{\left(x^{2}+y^{2}\right)^{3 / 2}}$
(b) $\frac{q}{2 \pi \varepsilon_{0}} \frac{d^{2}}{\left(x^{2}+y^{2}\right)^{3 / 2}}$
(c) 0
(d) $\frac{q}{4 \pi \varepsilon_{0}} \frac{d^{2}}{\left(x^{2}+y^{2}\right)^{1 / 2}}$

Q12. In an infinite fluid of density $\rho$ there are two spherical gas bubbles of radii $r_{1}$ and $r_{2}$ respectively. The gas has density $\rho_{g}<\rho$. The centres of the bubbles are separated by a distance $R \gg r_{1}, r_{2}$. If the space has no other forces than gravity, the bubbles will:
(a) Move towards each other due to an attractive gravitational force

$$
F=G\left(\rho-\rho_{g}\right)^{2}\left(\frac{4 \pi}{3}\right)^{2} \frac{r_{1}^{3} r_{2}^{3}}{R^{2}}
$$

(b) Move towards each other due to an attractive gravitational force

$$
F=G\left(\rho-\rho_{g}\right)^{2}\left(\frac{4 \pi}{3}\right) \frac{r_{1}^{3} r_{2}^{3}}{R^{2}}
$$

(c) Move away from each other due to a repulsive gravitational force

$$
F=G\left(\rho-\rho_{g}\right)^{2}\left(\frac{4 \pi}{3}\right)^{2} \frac{r_{1}^{3} r_{2}^{3}}{R^{2}}
$$

(d) Move away from each other due to a repulsive gravitational force

$$
F=G\left(\rho-\rho_{g}\right)^{2}\left(\frac{4 \pi}{3}\right) \frac{r_{1}^{3} r_{2}^{3}}{R^{2}}
$$

CSIR NET-JRF, GATE, IIT-JAM, JEST, TIFR and GRE for Physics
Q13. A mass of $M \mathrm{~kg}$ of water at temperature $T_{a}$ is isobarically and adiabatically mixed with an equal mass of water at temperature $T_{b}$. The specific heat of water at constant pressure is $C_{p}$. What is the entropy change $(\Delta S)$ of the system?
(a) $\Delta S=M C_{p} \ln \left\{1+\frac{\left(T_{a}-T_{b}\right)^{2}}{4 T_{a} T_{b}}\right\}$
(b) $\Delta S=M C_{p} \ln \left\{1-\frac{\left(T_{a}+T_{b}\right)^{2}}{4 T_{a} T_{b}}\right\}$
(c) $\Delta S=M C_{p} \ln \left\{1+\frac{\left(T_{a}+T_{b}\right)^{2}}{\left(T_{a}-T_{b}\right)^{2}}\right\}$
(d) $\Delta S=M C_{p} \ln \left\{\frac{T_{a}+T_{b}}{\sqrt{T_{a} T_{b}}}\right\}$

Q14. A string has 8 beads in a row, with $n$ identical red beads and $(8-n)$ identical blue beads. When one of the red beads is replaced by a blue one, the entropy of the given system changes from $S$ to $S+k_{B} \ln 2$. All configurations of the beads are equally probable. What is the value of $n$ ?
(a) 6
(b) 2
(c) 4
(d) 8

Q15. An ideal gas on the Pressure $(P)$ Volume $(V)$ diagram can be taken from point $K$ to point $N$ along three different paths, as shown below. $K \rightarrow L \rightarrow N, K \rightarrow N$, and $K \rightarrow M \rightarrow N$. Which of the following options is a true statement?

(a) The change in internal energy is the same along each path
(b) The same work is done along each path
(c) The same amount of heat is added to each the gas along each path
(d) There is no work done along the path $K \rightarrow N$

Q16. A technician receives an electronic instrument on which the following circuit diagram is drawn. Based on the shown timing diagram (binary values at pins 1, 2, 3, 4, 5 as a function of time) measured by the technician, identify the fault in the instrument.


Electronic circuit diagram
(a) An AND gate is used where an OR gate should have been used
(b) Input inverter acts like an OR gate
(c) Pin 4 shorted to ground
(d) Output inverter is faulty

Q17. The minimum number of two input NAND gates required to obtain the output $Y=\bar{A} B+\bar{C}$ from three inputs $A, B$ and $C$ is:
(a) 3
(b) 7
(c) 4
(d) 6

Q18. A student measures the radioactive decay of a material with a half-life of 13,000 years with a Geiger counter. In the laboratory notebook, the student records the following number of decays every 10 seconds:
$158,146,145,163,154,163,160,160,152,157,154,156,149,168,152$
The teacher suspects that the experiment was not done properly and the student created the numbers manually.

Why would the teacher have such a suspicion?
(a) The variance is much less than the mean, unlike what is expected for a Poisson distribution.
(b) The standard deviation is much less than the variance, as expected for a Poisson distribution.
(c) The median is less than the mean, unlike what is expected for a Poisson distribution.
(d) The median is greater than the mean, as expected for a Poisson distribution.

CSIR NET-JRF, GATE, IIT-JAM, JEST, TIFR and GRE for Physics
Q19. Unpolarised light of intensity $200 \mathrm{~W} / \mathrm{m}^{2}$ is incident on a set of two perfect polarisers arranged one behind the other. The first polariser has its transmission axis at $+55^{\circ}$ with respect to the vertical and the second polariser has its transmission axis at $+100^{\circ}$ with respect to the vertical. What is the intensity of the transmitted light?
(a) $50 \mathrm{~W} / \mathrm{m}^{2}$
(b) $100 \mathrm{~W} / \mathrm{m}^{2}$
(c) $1.98 \mathrm{~W} / \mathrm{m}^{2}$
(d) $3.01 \mathrm{~W} / \mathrm{m}^{2}$

Q20. Two small loudspeakers $A$ and $B$, separated by 15 cm , were pointed toward a small microphone $M$ at a distance 1.5 m away from the centre of the line $A B$, in the perpendicular direction as shown in the sketch below.


The following sound intensity pattern was observed as a function of the position of the microphone as it is moved parallel to AB.

The dips in the signal were repeated at the interval of 14.5 cm . The speed of sound in the experiment's background condition is $343 \mathrm{~m} / \mathrm{s}$. What can we conclude from this information?

(a) The two loudspeakers are vibrating at frequency 23.65 kHz and they are out of phase.
(b) The two loudspeakers are vibrating at frequency 23.65 kHz and they are in phase.
(c) The two loudspeakers are vibrating at frequency 47.3 kHz and they are in phase.
(d) The two loudspeakers are vibrating at frequency 47.3 kHz and they are out of phase.

CSIR NET-JRF, GATE, IIT-JAM, JEST, TIFR and GRE for Physics
Q21. The ionization potential of the $H$ atom is 13.598 eV . If the mass of a proton is $1.673 \times 10^{-27} \mathrm{~kg}$, the mass of an electron is $9.109 \times 10^{-31} \mathrm{~kg}$ and the mass of the $D$ nucleus is $3.3344 \times 10^{-27} \mathrm{~kg}$, the ionization potential of the $D$ atom is given by:
(a) 13.602 eV
(b) 13.594 eV
(c) 13.598 eV
(d) 27.188 eV

Q22. Consider a spaceship $S$ of length $L$ is moving relativistically in the $x$ direction with a speed $v_{x}$ relative to an inertial reference frame $F$ as shown in the figure. In $S$, a light bulb is placed at the left end (point $A$ ) and a detector is placed at the right end (point $B$ ). What is the time taken for light to travel from $A$ to $B$ in the reference frame $F$ ?

(a) $\frac{L}{c} \sqrt{\frac{1+v_{x} / c}{1-v_{x} / c}}$
(b) $\frac{L}{c} \sqrt{1-\frac{v_{x}^{2}}{c^{2}}}$
(c) $\frac{L}{c} \sqrt{\frac{1-v_{x} / c}{1+v_{x} / c}}$
(d) $\frac{L}{c} \frac{1}{\sqrt{1-v_{x}^{2} / c^{2}}}$

Q23. A beam of neutrons is incident normally upon a thick sheet of Cadmium. The mass density of Cadmium is $\rho=8.6 \mathrm{~g} \mathrm{~cm}^{-3}$. The absorption cross-section of neutrons on Cadmium nuclei is $2.5 \times 10^{-20} \mathrm{~cm}^{2}$. The atomic weight of Cadmium is known to be $112.40 \mathrm{~g} / \mathrm{mol}$. You may take $N_{A}=6.02 \times 10^{23}$.

At what depth is the intensity of the beam reduced by a factor $1 / e$ ?
(a) $9 \mu \mathrm{~m}$
(b) 9 fm
(c) 9 nm
(d) 900 fm

CSIR NET-JRF, GATE, IIT-JAM, JEST, TIFR and GRE for Physics
Q24. An electron confined in a two-dimensional square box, is in the ground state. The length of the side of this square is unknown, but it is seen that the electron jumps to the first excited energy state by absorbing electromagnetic radiation of wavelength 4,040 . What is the length of one side of the square well?
(a) 1.91 nm
(b) 1.68 nm
(c) 2.55 nm
(d) 3.82 nm

Q25. A student designed a new semiconductor with lattice constant $a$ that crystallizes in the facecentered cubic $(f c c)$ structure. The conduction band minimum of this semiconductor lies at all momentum points equivalent to $\vec{k}=(0.5,00) \pi / a$. How many conduction band minimum points are inside the first Brillouin zone?
(a) 6
(b) 4
(c) 3
(d) 1

## Section C

Q1. Consider the following matrix

$$
M=\left(\begin{array}{cccc}
1 & 5 & -7 & 1 \\
1 & 0 & 2 & 2 \\
9 & -1 & 3 & 1 \\
9 & 6 & -7 & -4
\end{array}\right)
$$

What is $\operatorname{det} e^{\mathrm{M}}$ ?
(a) 1
(b) $e$
(c) $e^{1210}$
(d) $e^{-1210}$

Q2. Let

$$
F(\lambda) \int_{-\infty}^{+\infty} d x e^{\lambda x-x^{2}}
$$

If the Taylor series expansion of $F(\lambda)$ around $\lambda=0$ is

$$
F(\lambda)=F_{0}+F_{1} \lambda+F_{2} \lambda^{2}+\cdots
$$

then the value of $F_{2}$ is
(You might find the following integral useful: $\int_{-\infty}^{+\infty} d x e^{-a x^{2}}=\sqrt{\frac{\pi}{a}}$ for $a>0$ )
(a) $\sqrt{\pi} / 4$
(b) $\sqrt{\pi} / 8$
(c) $\sqrt{\pi} / 2$
(d) $\sqrt{\pi}$

Q3. A horizontal constant force $F$ is applied on a uniform disc placed on a horizontal surface. The mass of the disc is $m$, and the radius is $r$. The point of application of $F$ is at a height $h(<2 r)$ from the surface. The disc starts from rest at $t=0$ and rolls without slipping. What is the speed of the centre of the disc at time $t$ ?

(a) $\frac{2 F h t}{3 m r}$
(b) $\frac{F t}{m}$
(c) $\frac{2 F t}{3 m}$
(d) $\frac{3 F h t}{2 m r}$

Q4. A particle of mass $m$ is attached to a massless string of length $L$. The other end of the string is fixed at a point $P$ as shown in the figure. $m$ moves under gravity and the tension of the string. The motion of the string is described using the generalized coordinates $\theta$ and $\phi$ which change with time. $\theta$ is the polar angle made by the string with the vertical and $\phi$ is the azimuthal angle made by the projection of the string on the $x y$ plane. The conjugate momenta to the variables $(\theta, \phi)$ are $\left(p_{\theta}, p_{\phi}\right)$, respectively.

Assuming that the string is tight throughout the motion, the Hamiltonian for the system is given by:

(a) $\frac{1}{2 m}\left[p_{\theta}^{2}+p_{\phi}^{2} \operatorname{cosec}^{2} \theta\right]+2 m g L \sin ^{2}\left(\frac{\theta}{2}\right)$
(b) $\frac{1}{2 m}\left[p_{\theta}^{2}+p_{\phi}^{2} \operatorname{cosec}^{2} \theta\right]-2 m g L \sin ^{2}\left(\frac{\theta}{2}\right)$
(c) $\frac{1}{2 m}\left[p_{\theta}^{2}+p_{\phi}^{2} \sin ^{2} \theta\right]+2 m g L \sin ^{2}\left(\frac{\theta}{2}\right)$
(d) $\frac{1}{2 m}\left[p_{\theta}^{2}+p_{\phi}^{2} \sin ^{2} \theta\right]-2 m g L \sin ^{2}\left(\frac{\theta}{2}\right)$

Q5. Consider $\hat{x}$ and $\hat{p}_{x}$ as the quantum mechanical position and linear momentum operators with eigenstates $|x\rangle$ and $\left|p_{x}\right\rangle$ and eigenvalues $x$ and $p_{x}$, respectively.

The eigenvalue of $\hat{x}$ acting on the state

$$
|\psi\rangle=e^{i \hat{p}_{x} a / 2 \hbar}|x\rangle
$$

(a) $x+\frac{a}{2}$
(b) $x-\frac{a}{2}$
(c) $x+a$
(d) $x-a$

CSIR NET-JRF, GATE, IIT-JAM, JEST, TIFR and GRE for Physics
Q6. A particle of mass $m$ moving in 1 dimension has the wavefunction

$$
\psi(x)=\frac{1}{\pi^{1 / 4} \sqrt{a}} e^{i p x / \hbar} e^{-x^{2} / 2 a^{2}}
$$

Its average kinetic energy is given by
(You might find the following integral useful: $\int_{-\infty}^{+\infty} d x e^{-a x^{2}}=\sqrt{\frac{\pi}{a}}$ for $a>0$ )
(a) $\frac{p^{2}}{2 m}+\frac{\hbar^{2}}{4 a^{2} m}$
(b) $\frac{\left(p+\frac{\sqrt{\pi} \hbar}{a}\right)^{2}}{2 m}$
(c) $\frac{\left(-p+\frac{\sqrt{\pi} \hbar}{a}\right)}{2 m}$
(d) $\frac{p^{2}}{2 m}+\frac{\hbar^{2}}{4 a^{2} m}+\frac{p \hbar}{2 m a}$

Q7. A smartphone emits electromagnetic radiation with a power of 1 Watt . What is the approximate value of the r.m.s. magnetic field at a distance 25 cm from the phone?
(a) $10^{-7}$ Tesla
(b) $10^{-5}$ Tesla
(c) $10^{-9}$ Tesla
(d) $10^{-11}$ Tesla

Q8. Each site of a linear chain of $N$ sites has a spin which can be in three different states with energies $0, \pm \varepsilon$, as shown in the figure below.


The system has a constraint that the neighbouring spins cannot be in the same state. At infinite temperature, the entropy of the system is given by:
(a) $N \ln 2+\ln \frac{3}{2}$
(b) $N \ln 3$
(c) $(N-1) \ln 2$
(d) $N \ln 2$

Q9. Consider a charge particle detection chamber as shown in the figure below. The chamber is made of a set of parallel plates separated by 20 mm distance and connected to the external resistance $(R=100 \Omega)$ as shown in the figure along with the high voltage power supply of 1 kV .


The chamber is filled with Argon ( Ar ) gas (ionization energy 16 eV ). If a charged particle passes through the chamber and loses sufficient energy, it ionizes the $A r$ atoms and generates a small voltage pulse across the resistance $R$.

In an experiment, an alpha particle of energy 5.5 MeV enters the chamber at a distance of 4 mm from the bottom plate, as shown, generating ion-electron pairs. If the effective capacitance of the chamber is 100 pF , the measured voltage pulse shape would be best described as:
(a) A sharp voltage pulse followed by a very weak broad pulse
(b) Two sharp voltage pulses of equal magnitude and opposite signs
(c) Two sharp voltage pulses of the same magnitude and sign
(d) No voltage pulse would be generated as both electrons and ions will neutralise the charge collected by the capacitor

Q10. A particular counting system has an average background rate of 50 counts $/ \mathrm{min}$. A decaying radioisotope source was introduced and the total 168 counts were measured in one minute. After a delay of 24 hrs , the system measured total 91 counts in one minute. If these measurements were used for determining the half-life $(\tau)$ of the source and if the average background rate, and the time have no errors, the $\%$ error $\left(100 \times \sigma_{\tau} / T\right)$ in the calculated halflife value due to counting statistics would be:
(a) $24.3 \%$
(b) $21.2 \%$
(c) $25.7 \%$
(d) $18.2 \%$

CSIR NET-JRF, GATE, IIT-JAM, JEST, TIFR and GRE for Physics
Q11. The Hamiltonian for a Helium atom is given as $H=H_{0}+H_{l}$, where

$$
H_{0}=\frac{\left(p_{1}^{2}+p_{2}^{2}\right)}{2 \mu}-\frac{2 e^{2}}{2 \pi \varepsilon_{0} r_{1}}-\frac{2 e^{2}}{4 \pi \varepsilon_{0} r_{2}}
$$

And

$$
H_{l}=\frac{e^{2}}{4 \pi \varepsilon_{0} r_{12}}
$$

where $\mu$ is the reduced mass of the electron, $r_{1}$ and $r_{2}$ are the distance of the electrons from the nucleus, and $r_{12}$ is the distance between the two electrons. The value of the first ionization potential of the Helium atom is 24.6 eV .

What is the correction due to $H_{l}$ to the ground state energy of the Helium atom, compared to $H_{0}$ ?
(a) 29.8 eV
(b) -29.8 eV
(c) 84.2 eV
(d) -2.6 eV

Q12. Oxygen $(O)$ nuclei $(Z=8)$ can be approximated as non-interacting protons and neutrons filling up orbitals in the following order.

$$
1 s_{1 / 2}, 1 p_{3 / 2}, 1 p_{1 / 2}, 1 d_{5 / 2}, 2 s_{1 / 2}, 1 d_{3 / 2}
$$

where the subscript specifies the $J$ quantum number. Given the binding energy of $O$ $(A=15)$ is $111.96 \mathrm{MeV}, O(A=16)$ is 127.62 MeV and $O(A=17)$, is 131.76 MeV what is the difference between the energies of the $1 p_{1 / 2}$ and the $1 d_{5 / 2}$ orbitals?
(a) 11.52 MeV
(b) 15.66 MeV
(c) 4.14 MeV
(d) 19.81 MeV

Q13. Consider a universe that always expands with a scale factor $a$ that increases with time as $a(t)=C t^{2 / 3}$ where $C$ is a constant. Its expansion rate at time $t$ is defined by the Hubble parameter

$$
H(t)=\frac{a}{a(t)} \frac{d a(t)}{d t}
$$

The current value of $H(t)$ in the universe is given by $H_{0}=975 \mathrm{kms}^{-1} \mathrm{Mpc}^{-1}$ where $1 M p c=3.1 \times 10^{22} \mathrm{~m}$. What is the approximate age of this universe?
(a) $10^{9}$ years
(b) $10^{7}$ years
(c) $10^{11}$ years
(d) $10^{13}$ years

## CSIR NET-JRF, GATE, IIT-JAM, JEST, TIFR and GRE for Physics

Q14. An $X$-ray of wavelength $3.1 \mathrm{~A}^{0}$ incident on the (110) plane of a cubic lattice with lattice constant $a$ produces a second-order Bragg reflection at $\theta=30^{\circ}$ ( $\theta$ is the angle measured from normal to the plane as shown in the figure).


What is the value of $a$ ?
(a) $5.06{ }^{0}$
(b) $8.77{ }^{\circ} \mathrm{A}$
(c) $3.58{ }^{\circ} \mathrm{A}$
(d) $5.46{ }^{\circ}$

Q15. Consider an unstable bound state $B$ of a proton $(p)$ with an antiproton $(\bar{p})$ which is in the $S$ state $(\ell=0)$ in the spin-singlet configuration. When this state $B$ decays, which of the following final states will NOT be possible?
(a) $\gamma+\gamma+\gamma$
(b) $\mu^{+}+\mu^{-}+\gamma$
(c) $\gamma+\gamma$
(d) $e^{+}+e^{-}+\gamma$

